

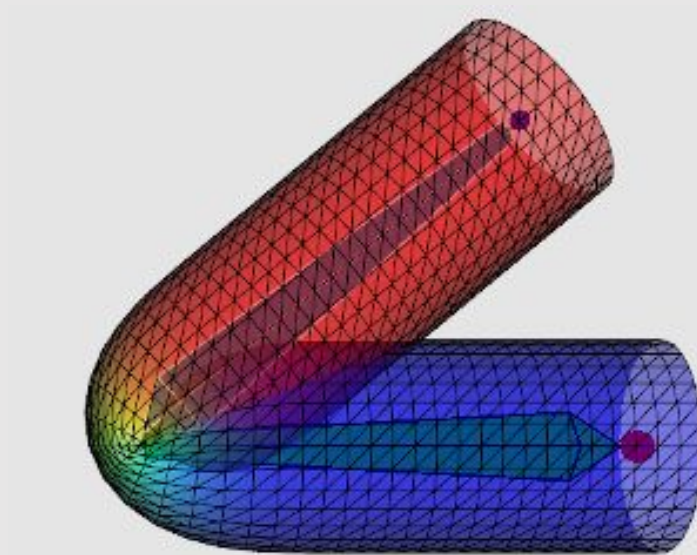
# A4.5: Skinning & Particles

- Linear Blend Skinning
- Particle Simulation

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# Linear Blend Skinning

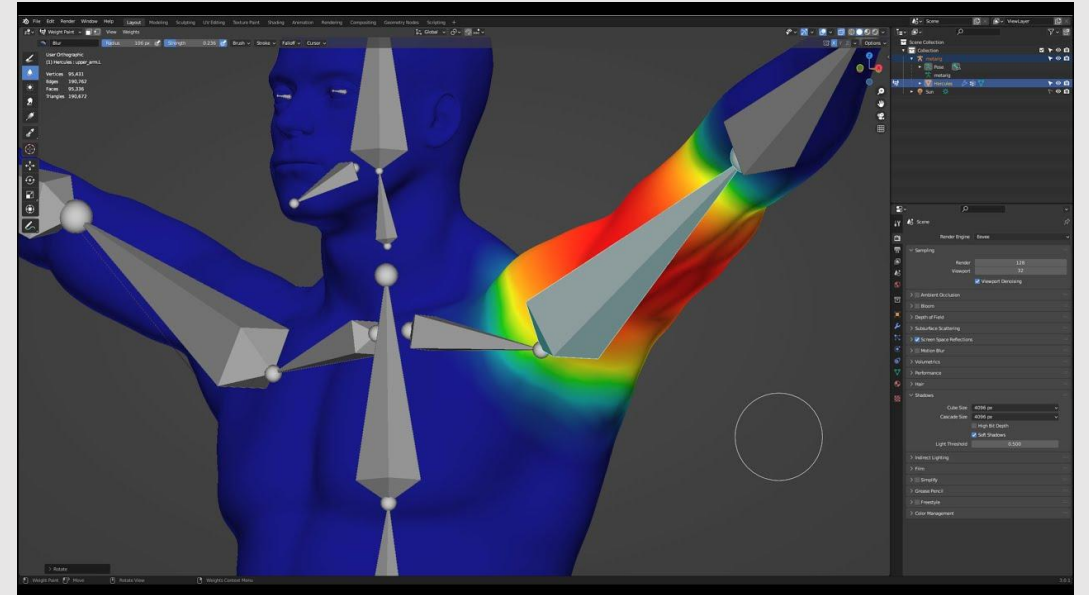
**Motivation:** We control how much the mesh geometry moves as the bones rotate by assigning each vertex a “weight” per bone



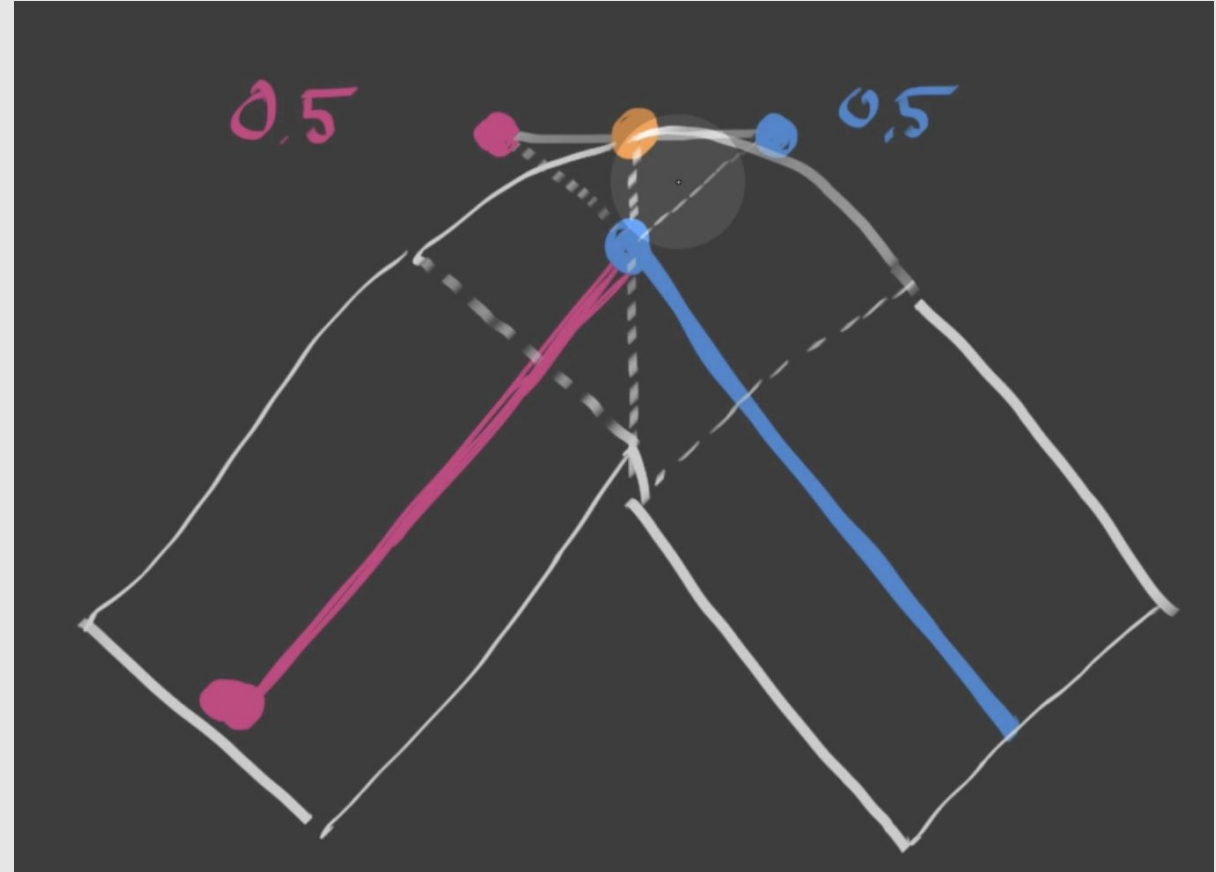
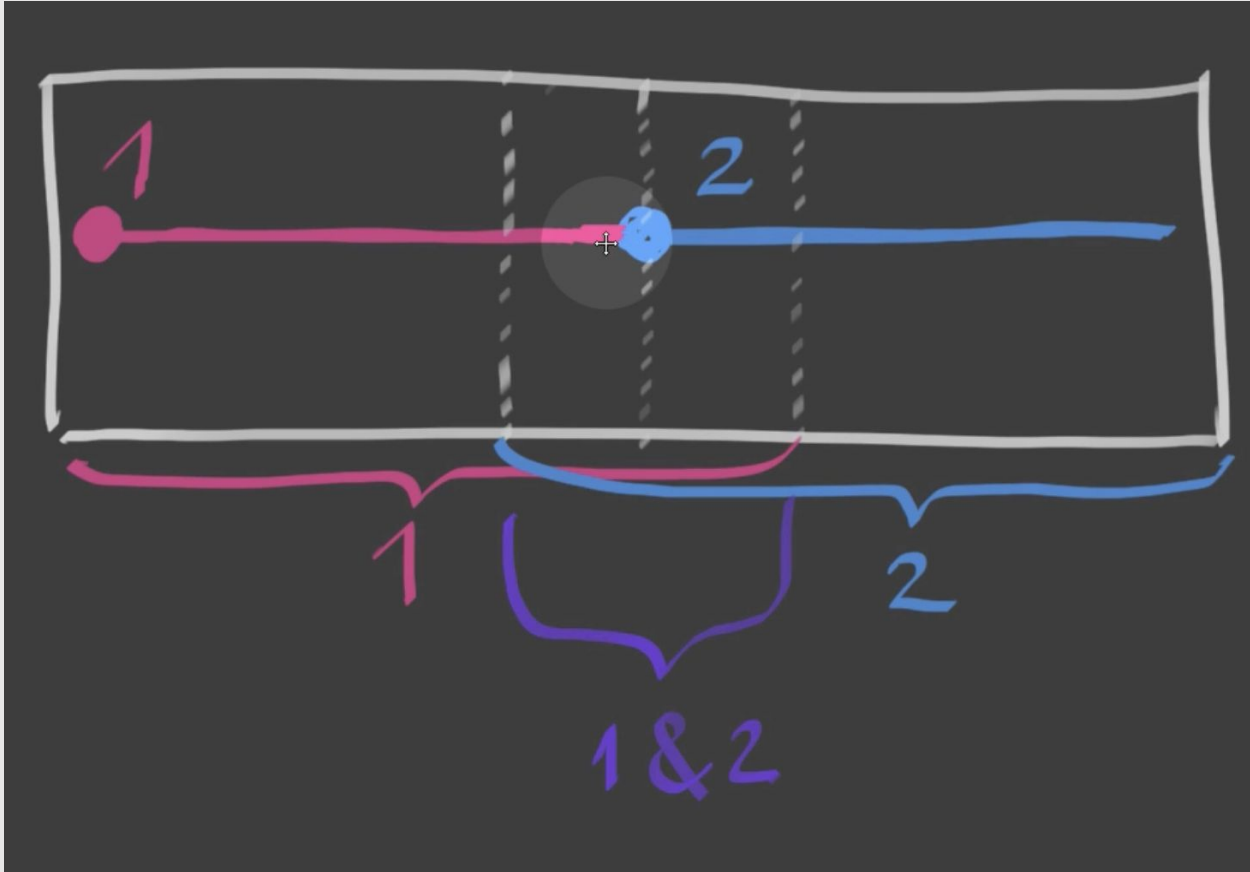
# Linear Blend Skinning

There are many ways one can assign these weights

- Manually - assign weights by having an artist “paint” the weights with a 3D program
- Automatically/Algorithmically
  - One method is Linear Blend Skinning, where we assign weights inversely proportional to the distance between the vertex and the bones

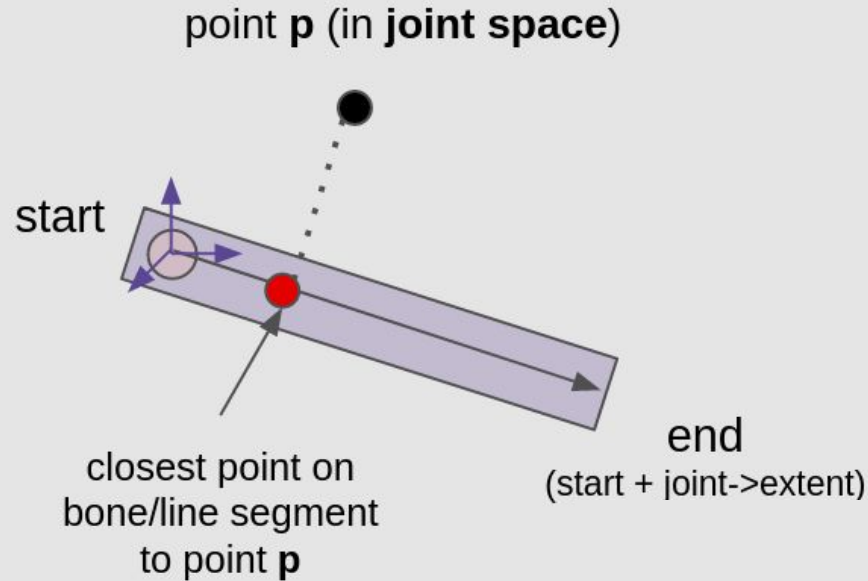


# Linear Blend Skinning



# Linear Blend Skinning

Weights assigned via inverse distance from vertex to the bone (represented by a line segment) up to a max distance define by bone::radius



For weight of vertex  $i$  with bone  $j$ ,  
and distance between the two given by  $d$ :

$$\hat{w}_{ij} \equiv \frac{\max(0, r - d_{ij})}{r}$$

Note : need to normalize per vertex so all weights add to one!

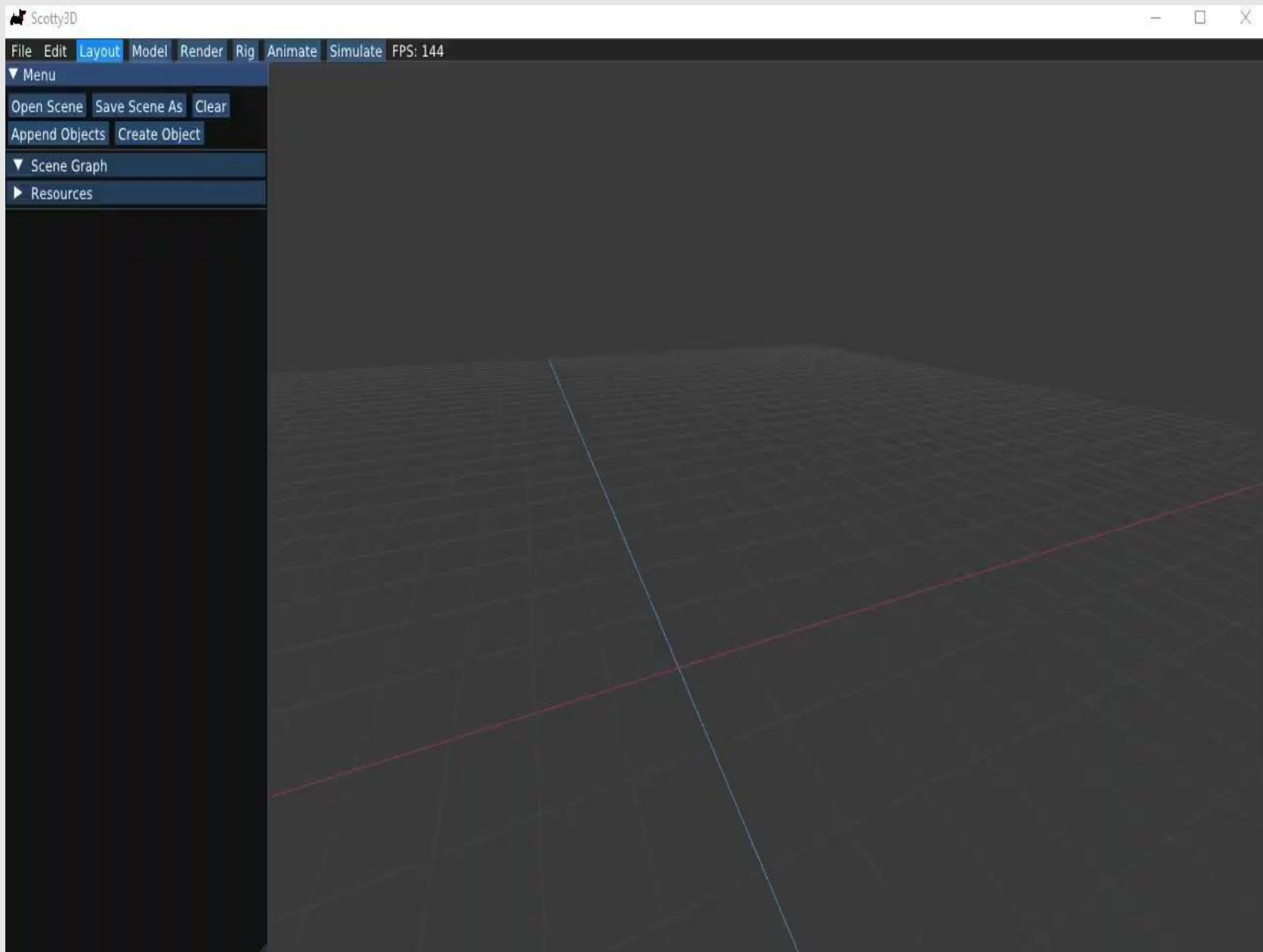
# Linear Blend Skinning

New vertex positions are thus a weighted sum of transformations under the bone transformations

- Transformations are from bind space (B) to pose space (P)

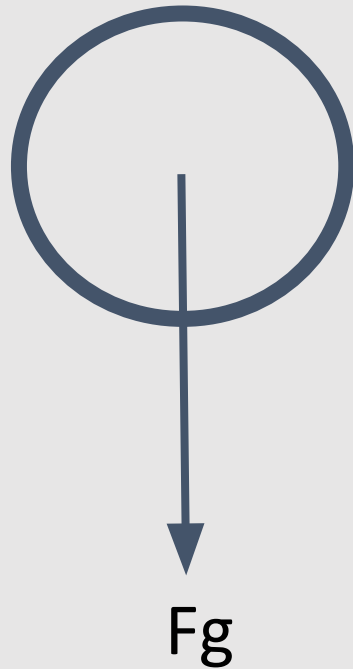
$$v'_i = \left( \sum_j w_{ij} P_j B_j^{-1} \right) v_i$$

- Linear Blend Skinning
- Particle Simulation



# Particles in Scotty3D

- Non-self-interacting, physics-simulated, spherical particles that interact with the rest of the scene
- Can use basic physics to simulate where a particle will be in the scene at a given time



$$F = ma$$
$$a = \frac{dv}{dt}$$
$$\frac{dv}{dt} = \frac{F}{m}$$
$$\frac{dx}{dt} = v$$

# Particles in Scotty3D

- Much easier to update position/velocity at small time-steps then continuously over a large time period
- Forward Euler
  - Can be unstable and does not conserve energy in a system – but that's ok for now
  - Means we evaluate function at our current configuration

$$\mathbf{x}_{t + \Delta t} = \mathbf{x}_t + \mathbf{v}_t \cdot \Delta T$$

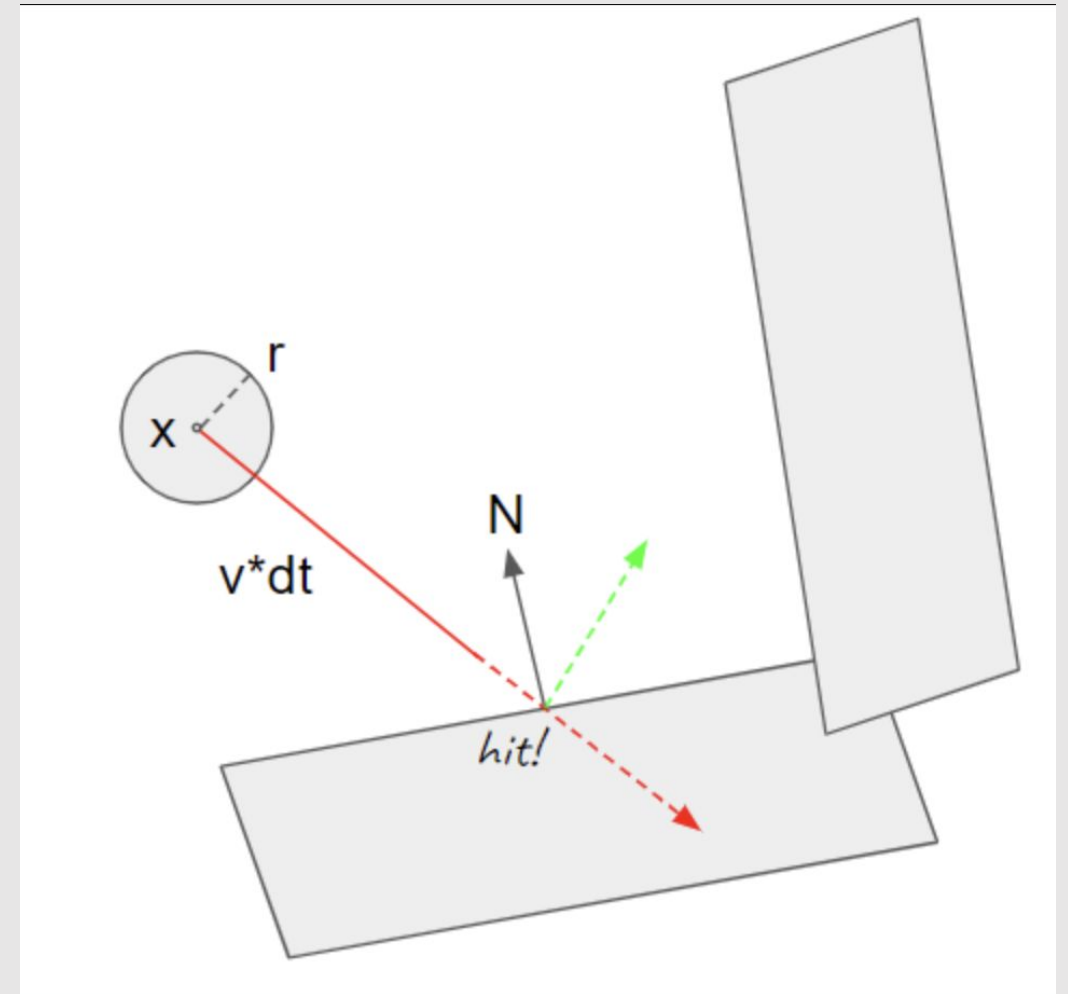
$$\mathbf{v}_{t + \Delta t} = \mathbf{v}_t + \mathbf{a} \cdot \Delta T$$

# Particle Collisions

- Can use Scotty3D's ray tracing (that you implemented!) to detect if particle collides with the scene within a timestep
  - Assume all particles collide elastically (i.e. a particle's velocity should be the same before and after a collision, with its direction reflected based on the surface normal)
  - Create a ray based on the particle's position and velocity
  - If the particles hits the scene within the current timestep
    - Reflect the velocity
  - Update velocity and position based on current timestep
  - Repeat until entire timestep is consumed

# Particle Collisions

- **If the particles hits the scene within the current timestep**
  - Reflect the velocity
- Note this is not as simple as checking if the ray hits something in the scene



# Pseudocode

```
void update_ball(Scene scene, Sphere *ball, float timestep) {

    Ray ray(ball->position, ball->velocity);
    bool hit = scene.hit(ray);

    if (hit)
    {
        bool hit_within_step = //TODO: does the hit happen within the timestep?
        float hit_time = //TODO: how much time does the hit take?

        if(hit_within_step)
        {
            ball->position += hit_time * ball->velocity;
            ball->velocity = // TODO: what will the new velocity be?
            // We may have another collision, so check again
            return update_ball(scene, ball, timestep - hit_time);
        }
    }
    // Update with forward Euler
    ball->position += timestep * ball->velocity;
    ball->velocity += timestep * scene.gravity;
}
```

# Note on Grading/Test Cases

- We only give you a few test cases
- In the past these tests have been flaky
- It's possible your implementation is 100% correct but a test fails
- Assess for correctness based on tests AND visually via the GUI
  - view expected behavior on Scotty3D docs/writeup
- We will grade your code visually as well
  - come to OH if you want to verify correctness
- Watch out for:
  - particles falling through walls
  - particles intersecting walls before bouncing

# Notes

- See [cmu-graphics.github.io/Scotty3D-docs/guide/animate\\_mode/](https://cmu-graphics.github.io/Scotty3D-docs/guide/animate_mode/) (Scotty3d docs) for instructions on how to make an animation
- Only ONE LATE DAY allowed for A4.5
  - regardless of how many late days you have left
- Final exam will be cumulative
  - Same format as midterm
  - Final review EITHER next recitation or in class Wednesday (TBD)
- All of you are awesome ... please apply to TA 15-362 next sem!!!
  - We have a specific form posted on Piazza (we don't look at applications from the CMU CS TA website)