# Perspective Projection & Rasterization

- Perspective Projection
- Drawing a Line
- Drawing a Triangle
- Supersampling



#### Perspective Projection



#### The Pinhole Camera



Our image seems to be upside down…

#### The Pinhole Camera



Better!...but what if part of our scene is closer that  $z < 1$ ?

#### The Pinhole Camera



We'll just go back to capturing content like this We can always flip the image at the end

#### Perspective Projection



#### Perspective Projection

![](_page_8_Figure_1.jpeg)

#### Camera Example

Consider camera at  $(4,2,0)$ , looking down x-axis, object given in world coordinates:

![](_page_9_Figure_2.jpeg)

**Goal:** find a spatial transformation for the object in a coordinate system where the camera is at the origin, looking down the –z axis

> **1) Translate by (-4,-2,0) 2) Rotate by 90deg about the y-axis**

#### Camera Example

Now consider a camera at the origin looking in a direction  $w \in \mathbb{R}^n3$ 

![](_page_10_Figure_2.jpeg)

#### View Frustrum

![](_page_11_Figure_1.jpeg)

**Q:** Why is it important we have a z-near and z-far?

#### Logarithmic Distance

- Objects get smaller at a logarithmic rate as they move farther from our eyes
	- In this class, **eyes == cameras**
	- Little change in size for objects already far away as they get farther
- In computer graphics, we quantize everything:
	- Colors
	- **Shapes**
	- Depth
- Providing a fixed precision for depth (usually 32 bits) means objects very far away may share the same depth data
	- Limited representable depth values
	- Leads to unintentional clipping

![](_page_12_Figure_11.jpeg)

Near and Far Clipping (2015) Udacity

#### Near and Far Clipping Planes

![](_page_13_Figure_1.jpeg)

Near and Far Clipping (2015) Udacity

![](_page_13_Figure_3.jpeg)

**floating point has more "resolution" near zero**

- **Idea:** set a smaller range for possible depth values
	- Min depth is the **near clipping plane**
	- Max depth is the **far clipping plane**
		- Logarithmic curve doesn't give many possible values for far objects…
- **Problem:** accidentally clip out objects important to our scene if range set too small
	- Near/Far clipping plane should encapsulate the most important objects closest/farthest to the camera
- **Advantage:** far clipping cuts out unimportant objects from your scene early in the pipeline
	- **Examples:** far-away trees in an already dense forest

# Clipping

- **Clipping** eliminates triangles not visible to the camera (not in view frustum)
	- Don't waste time rasterizing primitives you can't see!
	- Discarding individual fragments is expensive
		- "Fine granularity"
	- Makes more sense to toss out whole primitives
		- "Coarse granularity"
- What if a primitive is **partially clipped?**
	- Partially enclosed triangles are tessellated into smaller triangles in the frustrum
- If part of a triangle is outside the frustrum, it means at least one of its vertices are outside the frustrum
	- **Idea:** check if vertices in frustrum  $\Box$  = in frustrum

![](_page_14_Figure_11.jpeg)

![](_page_15_Figure_0.jpeg)

#### Map Frustrum To Cube

subtract the midpoint to center the coordinate

$$
A = \begin{bmatrix} \frac{2}{r-l} & 0 & 0 & \frac{l+r}{l-r} \\ 0 & \frac{2}{t-b} & 0 & \frac{b+t}{b-t} \\ 0 & 0 & \frac{2}{n-f} & \frac{f+n}{f-n} \\ 0 & 0 & 0 & 1 \end{bmatrix}
$$
  
[**translate terms**]  
[**scale terms**]

 $\chi$  –  $l+r$ 2

divide by the clipping range to normalize to [-0.5, 0.5]

 $\chi$  $r-l$ −  $l+r$  $2(r-l)$ 

scale by 2 to expand range to [-1, 1]

$$
\frac{2x}{r-l} - \frac{l+r}{r-l}
$$

- **Q:** why is the z-axis scalar term  $\frac{2}{n-f}$ ?
	- Camera looks down –z axis, so we need to flip axis!

flip sign of second fraction to make translation additive

$$
\frac{2}{r-l}x + \frac{l+r}{l-r}
$$

![](_page_17_Figure_1.jpeg)

With perspective projection, we end up dividing out the z coordinate. Full perspective matrix takes geometry of view frustum into account:

![](_page_17_Figure_3.jpeg)

$$
\begin{bmatrix}\n\frac{2n}{r-l} & 0 & \frac{r+l}{r-l} & 0 \\
0 & \frac{2n}{t-b} & \frac{t+b}{t-b} & 0 \\
0 & 0 & \frac{-(f+n)}{f-n} & \frac{-2fn}{f-n} \\
0 & 0 & -1 & 0\n\end{bmatrix}
$$

![](_page_18_Figure_1.jpeg)

$$
\begin{bmatrix} 1 & 0 & 0 & 0 \ 0 & 1 & 0 & 0 \ 0 & 0 & 1 & 0 \ 0 & 0 & 1 & 0 \ \end{bmatrix} \begin{bmatrix} x \ y \ z \ w \end{bmatrix} = \begin{bmatrix} x \ y \ z \ z \end{bmatrix} \longrightarrow \begin{bmatrix} x/z \ y/z \ 1 \ 1 \end{bmatrix}
$$

**Same idea as above:** w divides out the depth, so we set it equal to the depth z **Small difference:** we are looking down the  $-z$  axis, so we set  $w = -z$ 

![](_page_19_Figure_1.jpeg)

![](_page_19_Figure_2.jpeg)

 $\overline{n}$  $-z$  $\chi$ 

use the same equation as before, subbing in new projection

![](_page_19_Picture_5.jpeg)

simplify first term, multiply  $z/z$  to second term

$$
\frac{2n}{(r-l)(-z)}x + \frac{(r+l)z}{(r-l)(-z)}
$$

extract –  $z$  from denominator

$$
\frac{\left(\frac{2n}{(r-l)}x + \frac{(r+l)}{(r-l)}z\right)}{-z}
$$

By setting  $w = -z$ , we will do this last division step

\*\*see [http://www.songho.ca/opengl/gl\\_projectionmatrix.html](http://www.songho.ca/opengl/gl_projectionmatrix.html) for a full derivation when dividing out the depth

![](_page_19_Figure_12.jpeg)

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 $\mathbf{\mathsf{L}}$ 

the final normalized  $z_n$  is a function of the initial z and w, divided by the negative depth (projection):

$$
z_n = \frac{Az + Bw}{-z}
$$

to solve for  $A$  and  $B$ , solve for the fact that -n maps to -1 and -f maps to 1\*\*

$$
\frac{-An + B}{n} = -1
$$

$$
\frac{-Af + B}{f} = 1
$$

2 equations, 2 unknowns, use your favorite linear solver

$$
A = \frac{-(f+n)}{f-n}
$$

$$
B = \frac{-2fn}{f - n}
$$

$$
\begin{bmatrix}\n\frac{2n}{r-l} & 0 & \frac{r+l}{r-l} & 0 \\
0 & \frac{2n}{t-b} & \frac{t+b}{t-b} & 0 \\
0 & 0 & \frac{-(f+n)}{f-n} & \frac{-2fn}{f-n} \\
0 & 0 & -1 & 0\n\end{bmatrix}
$$

$x_1 = \{l, b, n, 1\}$	$y_1 = \{-1, -1, 1, 1\}$
$x_2 = \{r, b, n, 1\}$	$y_2 = \{1, -1, 1, 1\}$
$x_3 = \{r, t, n, 1\}$	$y_3 = \{1, 1, 1, 1\}$
$x_4 = \{l, t, n, 1\}$	$y_4 = \{-1, 1, 1, 1\}$
$x_5 = \{l, b, f, 1\}$	$y_5 = \{-1, -1, -1, 1\}$
$x_6 = \{r, b, f, 1\}$	$y_6 = \{1, -1, -1, 1\}$
$x_7 = \{r, t, f, 1\}$	$y_7 = \{1, 1, -1, 1\}$
$x_8 = \{l, t, f, 1\}$	$y_8 = \{-1, 1, -1, 1\}$

\*\*remember w is a homogeneous coordinate, so w=1

 $\Gamma$ 

#### Screen Transform

- We now have a way of going from camera view frustrum to normalized screen space:
	- Apply projection matrix
	- Divide out w-coordinate (set to  $-z$ )
- Last transform: image space
	- Take points from  $[-1,1] \times [-1,1]$  to a W x H pixel image
- Step 1: reflect about x-axis
- Step 2: translate by  $(1,1)$
- Step 3: scale by  $(W/2, H/2)$

![](_page_21_Figure_9.jpeg)

#### Perspective Projection

![](_page_22_Figure_1.jpeg)

Image flipped upside down.

#### Rasterization

- **Problem:** displays don't know what a triangle is or how to display one
	- But they do know how to display a buffer of pixels!
- **Goal:** convert draw instructions into an image of pixels to show on the display
	- Example: **color**

<polygon fill="#ED18ED"

points="464.781,631.819 478.417,309.091 471.599,642.045 "/>

**3 x (2D points)**

- The above is a valid svg instruction
- Requires turning shapes into pixels
	- Need to check which shapes overlap which pixels

![](_page_23_Figure_11.jpeg)

Direct3D Documentation (2020) Microsoft

#### Rasterization

For Each **Triangle**: For Each **Pixel**: If **Pixel** In **Triangle**: Pixel Color = Triangle Color

- How to check if a pixel is inside a triangle?
- A pixel is a little square, check if the square exists inside the triangle\*\*
	- Expensive/hard to compute!
- A pixel is a point, check if the point exists inside the triangle
	- Put the point at the pixel's center
	- We will refer to these as half-integer coordinates (Ex: [1.5, 4.5])

![](_page_24_Figure_8.jpeg)

![](_page_24_Figure_9.jpeg)

\*\**"A pixel is not a little square"* Alvy Ray Smith

- Perspective Projection
- Drawing a Line
- Drawing a Triangle
- Supersampling

Before that, Let's learn how to draw a line!

Surely it can't be difficult…it's just a line

#### Introduction To The Line

- A line is defined by  $(x_1, y_1)$ ,  $(x_2, y_2)$ 
	- Slope given as  $m = \frac{\tilde{y}_2 \tilde{y}_1}{\tilde{x}_1 \tilde{y}_2}$  $x_2-x_1$
- What does it mean for a line to overlap a pixel?
	- A pixel is just a point
	- A line has no thickness
		- Neither have a notion of area
- Instead, we will reinterpret pixels as squares
	- A pixel lights up if the line intersects it
		- Checking if a line intersects a pixel can be expensive!
- Find a linear algorithm  $\sim O(n)$  where n is the number of output fragments
	- Everything we check should be everything in the output

![](_page_27_Figure_12.jpeg)

#### The Bresenham Line Algorithm

- Consider the case when  $m$  is in range [0,1]
	- Implies  $\Delta x \geq \Delta y$
- We will traverse up the x-axis
	- Each step of x we take, decide if we keep y the same or move y up one step
		- Since  $0 < m < 1$ , a positive move in x causes a positive move in y

#### **[ pseudocode ] [ code ]**

Ensure the x-coordinate of  $(x_1, y_1)$  is smaller Let y' be our current vertical component along the line Let y be the initial  $y_1$ 

For each x value in range  $[x_1, x_2]$  with step 1:

#### Shade (x, y)

 Add m to y' (if x takes step 1, y' takes step m) If the new y' is closer to the row of pixels above: Add 1 to y

![](_page_28_Figure_11.jpeg)

If 
$$
x_1 > x_2
$$
:  
\n
$$
Swap(x_1, x_2), \quad Swap(y_1, y_2)
$$
\n
$$
\varepsilon \leftarrow 0, \quad y \leftarrow y_1
$$
\nFor  $x \leftarrow x_1$  to  $x_2$  do:  
\n
$$
Shade(x, y)
$$
\nIf  $(|\varepsilon + m| > 0.5)$ :  
\n
$$
\varepsilon \leftarrow \varepsilon + m - 1, \quad y \leftarrow y + 1
$$
\nElse:  
\n
$$
\varepsilon \leftarrow \varepsilon + m
$$

#### The Bresenham Line Algorithm

• What if  $m$  is in range  $[0,1]$ ?

$$
\varepsilon \leftarrow 0, \quad y \leftarrow y_1
$$
  
For  $x \leftarrow x_1$  to  $x_2$  do:  
Shade $(x, y)$   
If  $(|\varepsilon + m| > 0.5)$ :  
 $\varepsilon \leftarrow \varepsilon + m - 1, \quad y \leftarrow y + 1$   
Else:  
 $\varepsilon \leftarrow \varepsilon + m$ 

• What if  $m > 1$ ?

$$
\varepsilon \leftarrow 0, \quad x \leftarrow x_1
$$
  
For  $y \leftarrow y_1$  to  $y_2$  do:  
Shade(x, y)  
If  $(|\varepsilon + 1/m| > 0.5)$ :  
 $\varepsilon \leftarrow \varepsilon + 1/m - 1, \quad x \leftarrow x + 1$   
Else:  
 $\varepsilon \leftarrow \varepsilon + 1/m$ 

- \*\*When traversing x-axis, x1 must be smaller. When traversing y-axis, y1 must be smaller
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• What if  $m$  is in range  $[-1,0]$ ?

```
\varepsilon \leftarrow 0, \quad y \leftarrow y_1For x \leftarrow x_1 to x_2 do:
     Shade(x, y)If (|\varepsilon + m| > 0.5):
          \varepsilon \leftarrow \varepsilon + m + 1, \quad y \leftarrow y - 1 Else:
          \varepsilon \leftarrow \varepsilon + m
```
• What if  $m < -1$ ?

$$
\varepsilon \leftarrow 0, \quad x \leftarrow x_1
$$
  
For  $y \leftarrow y_1$  to  $y_2$  do:  
Shade(x, y)  
If  $(|\varepsilon + 1/m| > 0.5)$ :  
 $\varepsilon \leftarrow \varepsilon + 1/m + 1, \quad x \leftarrow x - 1$   
Else:  
 $\varepsilon \leftarrow \varepsilon + 1/m$ 

![](_page_30_Picture_0.jpeg)

That's kinda complicated… Can we make it easier somehow?

#### The [Nicer] Bresenham Line Algorithm

![](_page_31_Picture_224.jpeg)

#### Introduction To The Line

- Bresenham algorithm only works if both the start and end coordinates lie on half-integer coordinates
- Instead we will consider a line to intersect a pixel if the line intersects the diamond inside the pixel
	- $|x p_x| + |y p_y| < \frac{1}{2}$ 2
		- Checks if point  $(x, y)$  lies in the diamond of pixel  $p$
- Still the same idea as before! The only difference is that we need to check if the endpoints correctly intersect the last pixels

![](_page_32_Figure_6.jpeg)

#### The [Even Nicer] Bresenham Line Algorithm

 $a = \langle x_1, y_1 \rangle, \quad b = \langle x_2, y_2 \rangle$  $\Delta x \leftarrow |x_2 - x_1|, \qquad \Delta y \leftarrow |y_2 - y_1|$ If  $(\Delta x > \Delta y)$ :  $i \leftarrow 0, \quad j \leftarrow 1$ If  $(\Delta x < \Delta y)$ :  $i \leftarrow 1, \quad j \leftarrow 0$ If  $(a_i > b_i)$ :  $swap(a, b)$  $t_1 \leftarrow floor(a_i), \qquad t_2 \leftarrow floor(b_i)$ For  $u \leftarrow t_1$  to  $t_2$  do:  $W \leftarrow \frac{(u+0.5) - a_i}{(b-a)}$  $(b_i - a_i)$  $v \leftarrow w * (b_i - a_i) + a_i$ Shade( $floor(u) + 0.5$ ,  $floor(v) + 0.5$ )

**TODO:** fix  $t_1$  and  $t_2$  to properly account for OR discard the two edge fragments if the endpoints  $a$  and  $b$  are inside the 'diamond' of the edge fragments

Remember: 
$$
|x - p_x| + |y - p_y| < \frac{1}{2}
$$

• Perspective Projection

• Drawing a Line

- Drawing a Triangle
- Supersampling

![](_page_35_Figure_0.jpeg)

![](_page_36_Figure_1.jpeg)

- Which points do we check?
	- **Idea 1:** check all points  $q$  in the image
		- For large images (1080p), we're checking hundreds of thousands of points per triangle!
	- $\cdot$  **Idea 2:** check all points  $q$  in the bounding box of the triangle:
		- $x_{min} = \min(a_x, b_x, c_x)$
		- $y_{min} = \min(a_y, b_y, c_y)$

• 
$$
x_{max} = max(a_x, b_x, c_x)
$$

- $y_{max} = \max(a_y, b_y, c_y)$
- How to check if a point is inside a triangle?

![](_page_37_Figure_1.jpeg)

- How to check if a point is inside a triangle?
- Check that  $q$  is on the  $b$  side of  $\overrightarrow{ac}$

$$
(\overrightarrow{ac} \times \overrightarrow{ab}) \cdot (\overrightarrow{ac} \times \overrightarrow{aq}) > 0
$$

![](_page_38_Figure_1.jpeg)

- How to check if a point is inside a triangle?
- Check that  $q$  is on the  $a$  side of  $\overrightarrow{cb}$

$$
(\overrightarrow{cb} \times \overrightarrow{ca}) \cdot (\overrightarrow{cb} \times \overrightarrow{cq}) > 0
$$

![](_page_39_Figure_1.jpeg)

- How to check if a point is inside a triangle?
- Check that  $q$  is on the  $c$  side of  $\overrightarrow{bc}$

$$
(\overrightarrow{ba} \times \overrightarrow{bc}) \cdot (\overrightarrow{ba} \times \overrightarrow{bq}) > 0
$$

![](_page_40_Figure_1.jpeg)

• How to check if a point is inside a triangle?

$$
(\overrightarrow{ac} \times \overrightarrow{ab}) \cdot (\overrightarrow{ac} \times \overrightarrow{aq}) > 0 && & \\ (\overrightarrow{cb} \times \overrightarrow{ca}) \cdot (\overrightarrow{cb} \times \overrightarrow{cq}) > 0 && & \\ (\overrightarrow{ba} \times \overrightarrow{bc}) \cdot (\overrightarrow{ba} \times \overrightarrow{bq}) > 0
$$

• What if b and c were swapped?

$$
(\overrightarrow{ab} \times \overrightarrow{ac}) \cdot (\overrightarrow{ac} \times \overrightarrow{aq}) < 0
$$

• Orientation matters!

![](_page_41_Figure_1.jpeg)

• **Measurements must all either be positive or negative** for point to be in triangle

$$
(\overrightarrow{ac} \times \overrightarrow{ab}) \cdot (\overrightarrow{ac} \times \overrightarrow{aq}) > 0 && k
$$
\n
$$
(\overrightarrow{cb} \times \overrightarrow{ca}) \cdot (\overrightarrow{cb} \times \overrightarrow{cq}) > 0 && k
$$
\n
$$
(\overrightarrow{ba} \times \overrightarrow{bc}) \cdot (\overrightarrow{ba} \times \overrightarrow{bq}) > 0
$$

OR  
\n
$$
(\overrightarrow{ab} \times \overrightarrow{ac}) \cdot (\overrightarrow{ac} \times \overrightarrow{aq}) < 0 && \& (\overrightarrow{ca} \times \overrightarrow{cb}) \cdot (\overrightarrow{cb} \times \overrightarrow{cq}) < 0 && \& (\overrightarrow{bc} \times \overrightarrow{ba}) \cdot (\overrightarrow{ba} \times \overrightarrow{bq}) < 0
$$

- Orientation no longer matters
	- Just be consistent!

#### Incremental Triangle Traversal

![](_page_42_Figure_1.jpeg)

$$
P_i = (x_i/w_i y_i/w_i z_i/w_i) = (X_i Y_i Z_i)
$$

$$
dX_i = X_{i+1} - X_i
$$
  

$$
dY_i = Y_{i+1} - Y_i
$$

$$
E_i(x, y) = (x - X_i)dY_i - (y - Y_i)dX_i
$$

 $E_i(x, y) = 0$ : point on edge  $E_i(x, y) > 0$ : point outside edge  $E_i(x, y) < 0$ : point inside edge

 $dE_i(x + 1, y) = E_i(x, y) + dY_i$  $dE_i(x, y + 1) = E_i(x, y) + dX_i$ 

#### Parallel Coverage Tests

![](_page_43_Figure_1.jpeg)

- Incremental traversal is very serial; modern hardware is highly parallel
	- Test all samples in triangle bounding box in parallel
- All tests share some 'setup' calculations
	- Computing  $\overrightarrow{ac}$ ,  $\overrightarrow{cb}$ ,  $\overrightarrow{ba}$
- Modern GPUs have special-purpose hardware for efficiently performing point-in-triangle tests
	- Same set of instructions, regardless of which coordinate  $q$  we are dealing with

#### Hierarchical Coverage Tests

![](_page_44_Figure_1.jpeg)

- **Idea:** work coarse-to-fine
	- Check if large blocks are inside the triangle
		- **Early-in:** every pixel is covered
		- **Early-out:** every pixel is not covered
		- **Else:** test each pixel coverage individually
- **Early-in:** if all 4 corners of the block are inside the triangle
- **Else:** if a triangle line intersects a block line
- **Early-out:** if neither **Early-in** nor **Else**
- **Careful!** Best to represent block as smallest bounding box to pixel samples, not the pixels themselves!

#### Hierarchical Coverage Tests

- What is the right block size?
	- **Too big:** very difficult to get an **Early-in** or **Early-out**
	- **Too small:** blocks are too similar to pixels
- **Idea:** create a hierarchy of block sizes
	- When entering the **Else** case, just drop down to the next smallest block size
	- Checking coverage reduced to logarithmic (We will learn why in a future lecture)

![](_page_45_Figure_7.jpeg)

• Perspective Projection

**• Drawing a Line** 

• Drawing a Triangle

• Supersampling

#### Pixel Coverage

Which triangles "cover" this pixel?

![](_page_47_Figure_2.jpeg)

#### Pixel Coverage

- Compute fraction of pixel area covered by triangle, then color pixel according to this fraction
	- **Ex:** a red triangle that covers 10% of a pixel should be 10% red
- Difficult to compute area of box covered by triangle
	- Instead, consider coverage as an approximation

![](_page_48_Figure_5.jpeg)

![](_page_49_Picture_0.jpeg)

#### Coverage Via Samples

- A **sample** is a discrete measurement of a signal
	- Used to **convert continuous data to discrete**, but we can also take **samples of discrete data** too
- The more samples we take, the more accurate the image becomes
	- Same idea as using a larger sensor to take a betterquality photo
- **Problem:** each sample adds more work
	- What is the best way to use the least amount of samples to best approximate the original scene?
		- Main idea of **sample theory**

## Sampling in 1D

![](_page_50_Figure_1.jpeg)

 $x_0$   $x_1$   $x_2$   $x_3$   $x_4$  $f'(x)$ 

- **Idea:** take 5 random samples along the domain and evaluate  $f(x)$ 
	- Many different ways to interpolate points:
		- Piecewise
		- Linear
		- Cubic
- Where is the best place to put 5 samples?
	- We know the answer because we can see the entire function  $f$ 
		- $\bullet$  f has been evaluated over the entire domain
	- What if we cannot see all of  $f$ ?
	- What if  $f$  is expensive to evaluate?

### Sampling in 1D

![](_page_51_Figure_1.jpeg)

- **Idea:** take more than 5 random samples along the domain and evaluate  $f(x)$ 
	- Gets a better reconstruction of  $f$  but...
		- More evaluation calls needed
		- More memory to save
- Still don't know the best way to interpolate samples
	- Need to guess based on the behavior of  $f$
	- Can consider things like gradients and such…

#### Pixel Coverage

Which triangles "cover" this pixel?

![](_page_52_Figure_2.jpeg)

 $\sum$  = triangle

#### Edge Case

![](_page_53_Figure_1.jpeg)

- When edge falls directly on a screen sample, the sample is classified as within triangle if the edge is a "top edge" or "left edge"
	- **Top edge:** horizontal edge that is above all other edges
	- **Left edge:** an edge that is not exactly horizontal and is on the left side of the triangle
		- Triangle can have one or two left edges
- This is known as **edge ownership**

Direct3D Documentation (2020) Microsoft

So how many samples do we take?

#### Sampling Per Pixel

![](_page_55_Figure_1.jpeg)

**Idea:** take as many samples as there are pixels on screen

![](_page_56_Figure_0.jpeg)

#### Aliasing Artifacts

- Imperfect sampling + imperfect reconstruction leads to image artifacts
	- Jagged edges
	- Moiré patterns
- Does this remind you of old school video games?
	- Old games took few samples and took few steps to prevent aliasing
		- Expensive to take more samples
		- Not enough compute to do filtering to interpolate samples
		- Not enough memory to take more samples

![](_page_57_Picture_9.jpeg)

#### Supersampling Per Pixel

![](_page_58_Figure_1.jpeg)

**Idea:** take many more samples than there are pixels on screen

![](_page_59_Figure_1.jpeg)

Each pixel now holds **n** samples. Average the **n** samples together to get **1** sample per pixel **(1spp).** 

![](_page_60_Figure_1.jpeg)

![](_page_61_Figure_1.jpeg)

![](_page_62_Figure_1.jpeg)

#### Supersampling Artifacts

![](_page_63_Figure_1.jpeg)

#### Supersampling Artifacts

![](_page_64_Picture_1.jpeg)

In special cases, we can compute the exact coverage. This occurs when what we are sampling matches our sampling pattern – **very rare!**